
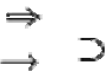









## List of Mathematical Symbols

Sl.no.	Symbols	Name	Explanation
1	$=$	is equal to; equals	$x = y$ means $x$ and $y$ do represent the same thing or value.
2	$\neq$	is not equal to; does not equal	$x \neq y$ means that $x$ and $y$ do not represent the same thing or value.
3	$<$ $>$	is less than, is greater than	$x < y$ means $x$ is less than $y$ . $x > y$ means $x$ is greater than $y$ .
4	$\ll$ $\gg$	is much less than, is much greater than	$x \ll y$ means $x$ is much less than $y$ . $x \gg y$ means $x$ is much greater than $y$ .
5	$\leq$ $\geq$	is less than or equal to, is greater than or equal to	$x \leq y$ means $x$ is less than or equal to $y$ . $x \geq y$ means $x$ is greater than or equal to $y$ .
6	$\prec$	is Karp reducible to; is polynomial-time many-one reducible to	$L_1 \prec L_2$ means that the problem $L_1$ is Karp reducible to $L_2$ .
7	$\propto$	is proportional to; varies as	$y \propto x$ means that $y = kx$ for some constant $k$ .
8	$+$	plus; add	$4 + 6$ means the sum of 4 and 6.
9	$-$	negative; minus; the opposite of	$9 - 4$ means the subtraction of 4 from 9.
10	$\times$	times; multiplied by	$3 \times 4$ means the multiplication of 3 by 4.
11	$\cdot$	times; multiplied by	$3 \cdot 4$ means the multiplication of 3 by 4.
12	$\div$ $/$	divided by; over	$6 \div 3$ or $6/3$ means the division of 6 by 3.
13	$\pm$	plus or minus	$6 \pm 3$ means both $6 + 3$ and $6 - 3$ .

14	$\mp$	minus or plus	$6 \pm (3 \mp 5)$ means both $6 + (3 - 5)$ and $6 - (3 + 5)$ .
15	$\sqrt{\quad}$	the (principal) square root of	$\sqrt{x}$ means the positive number whose square is $x$ .
16	$ \dots $	absolute value of; modulus of	$ \mathbf{x} - \mathbf{y} $ means the Euclidean distance between $\mathbf{x}$ and $\mathbf{y}$ .
17	$\ \dots\ $	norm of; length of	$\ x\ $ means the norm of the element $x$ of a normed vector space.
18	$\mid \nmid$	divides	$a \mid b$ means $a$ divides $b$ .  $a \nmid b$ means $a$ does not divide $b$ .
19	$\parallel$	is parallel to	$x \parallel y$ means $x$ is parallel to $y$ .
20	$\#$	cardinality of; size of; order of	$A \# B$ is the connected sum of the manifolds $A$ and $B$ . If $A$ and $B$ are knots, then this denotes the knot sum, which has a slightly stronger condition.
21	$\aleph$	aleph	$\aleph_\alpha$ represents an infinite cardinality  (specifically, the $\alpha$ -th one, where $\alpha$ is an ordinal).
22	$\beth$	beth	$\beth_\alpha$ represents an infinite cardinality  (similar to $\aleph$ , but $\beth$ does not necessarily index all of the numbers indexed by $\aleph$ ).

23	$\mathfrak{c}$	cardinality of the continuum; cardinality of the real numbers; $c$ ;	$\mathfrak{R} \mathfrak{R} \mathfrak{c}$ The cardinality of is denoted by or by the symbol (a lowercase Fraktur letter C).
24	$\therefore$	such that; so that	$\therefore$ means “such that”, and is used in proofs and the set-builder notation (described below).
25	$!$	factorial	$n!$ means the product $1 \times 2 \times \dots \times n$ .
26	$\sim$	has distribution	$X \sim D$ , means the random variable $X$ has the probability distribution $D$ .
27	$\approx$	is approximately equal to	$x \approx y$ means $x$ is approximately equal to $y$ .
28	$\wr$	wreath product of ... by ...	$A \wr H$ means the wreath product of the group $A$ by the group $H$ .
29	$\triangleleft$	is a normal subgroup of	$N \triangleleft G$ means that $N$ is a normal subgroup of group $G$ .
30	$\rtimes$ $\ltimes$	the semidirect product of	$N \rtimes_{\varphi} H$ is the semidirect product of $N$ (a normal subgroup) and $H$ (a subgroup), with respect to $\varphi$ . Also, if $G = N \rtimes_{\varphi} H$ , then $G$ is said to split over $N$ .
31	$\bowtie$	the natural join of	$R \bowtie S$ is the natural join of the relations $R$ and $S$ , the set of all combinations of tuples in $R$ and $S$ that are equal on their common attribute names.
32	$\therefore$	therefore; so; hence	Sometimes used in proofs before logical consequences.
33	$\because$	because; since	Sometimes used in proofs before reasoning.

34		QED; tombstone; Halmos symbol	Used to mark the end of a proof.
35		implies; if ... then	$A \Rightarrow B$ means if $A$ is true then $B$ is also true; if $A$ is false then nothing is said about $B$ .
36		if and only if; iff	$A \Leftrightarrow B$ means $A$ is true if $B$ is true and $A$ is false if $B$ is false.
37		not	The statement $\neg A$ is true if and only if $A$ is false.
38		and; min; meet	The statement $A \wedge B$ is true if $A$ and $B$ are both true; else it is false.
39		or; max; join	The statement $A \vee B$ is true if $A$ or $B$ (or both) are true; if both are false, the statement is false.
40		$x$ or	The statement $A \oplus B$ is true when either $A$ or $B$ , but not both, are true. $A \veebar B$ means the same.
41		for all; for any; for each	$\forall x: P(x)$ means $P(x)$ is true for all $x$ .
42		there exists; there is; there are	$\exists x: P(x)$ means there is at least one $x$ such that $P(x)$ is true.

43	$\exists!$	there exists exactly one	$\exists! x: P(x)$ means there is exactly one $x$ such that $P(x)$ is true.
44	$:=$ $\equiv$ $\Leftrightarrow$ $\triangleq$ $\stackrel{\text{def}}{=}$ $\stackrel{\text{def}}{=}$	is defined as; equal by definition	$x := y$ , $x =: y$ or $x \triangleq y$ means $x$ is defined to be another name for $y$ , under certain assumptions taken in context.
45	$\cong$	is congruent to	$G \cong H$ means that group $G$ is isomorphic (structurally identical) to group $H$ .
46	$\equiv$	... is congruent to ... modulo ...	$a \equiv b \pmod{n}$ means $a - b$ is divisible by $n$
47	$\{ , \}$	the set of ...	$\{a,b,c\}$ means the set consisting of $a$ , $b$ , and $c$ .
48	$\{ : \}$ $\{   \}$	the set of ... such that	$\{x : P(x)\}$ means the set of all $x$ for which $P(x)$ is true. $\{x   P(x)\}$ is the same as $\{x : P(x)\}$ .
49	$\emptyset$ $\emptyset$ $\{\}$	the empty set	$\emptyset$ means the set with no elements. $\{\}$ means the same.
50	$\in$ $\notin$	is an element of; is not an element of	$a \in S$ means $a$ is an element of the set $S$ ; $a \notin S$ means $a$ is not an element of $S$ .